

# **MATH 124 Spring 2005**

**Lecture: 23 A**

**Date: May 17, 2005**

**Skills you should acquire from this lecture:**

- Problem solving skills related to two sample problems for difference between two means. Confidence intervals and Hypothesis testing
- Problems 7.109, 7.117, 7.107, 7.110(a,b,c)

problems related to difference between two means

7.109, 7.117, 7.107, 7.110a, b, c

### Problem 7.109

Let  $\mu_1$  = mean amino acid uptake of nitrate labelled medium

$\mu_2$  = mean amino acid uptake of control medium

$H_0: \mu_1 - \mu_2 \geq 0$  (ie amino acids ~~uptake~~ <sup>uptake</sup> same or higher for nitrate)

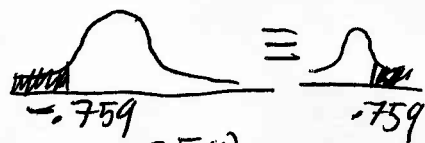
$H_A: \mu_1 - \mu_2 < 0$  (ie amino acid uptake lower for nitrates)

test statistic 
$$t = \frac{7880 - 8112}{\sqrt{\frac{1115^2}{30} + \frac{1250^2}{30}}} = -0.759 \text{ (3dp)}$$

with  $df = \min(30-1, 30-1) = 29$

since  $H_A$  is  $\mu_1 - \mu_2 < 0$

$P\text{-value} = P(T < -0.759)$



by symmetry of  $t$  distribution  $P(T < -0.759) = P(T > 0.759)$

so  $.683 < .759 < .854$

$\Rightarrow .25 > P(T > .759) > .20$

since  $P\text{-value}$  is large cannot reject  $H_0$ . There is no evidence to show that nitrates decrease amino acid uptake.

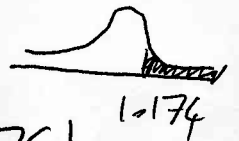
## Problem 7.117

Let  $\mu_1$  = mean cholesterol level of ~~plate~~ dogs  
 $\mu_2$  = mean cholesterol level of clinic dogs

(a)  $H_0: \mu_1 - \mu_2 \leq 0$  (CIC pets have same or lower cholesterol than clinic dogs)  
 $H_A: \mu_1 - \mu_2 > 0$  (CIC pets have higher cholesterol)

$$\text{test statistic } t = \frac{193 - 174}{\sqrt{\frac{68^2}{26} + \frac{44^2}{23}}} = 1.174 \text{ (3dp)}$$

with  $df = \min(26-1, 23-1) = 22$



Since  $H_A$  is  $\mu_1 - \mu_2 > 0$   $P\text{-value} = P(T > 1.174)$

$$1.061 < 1.174 < 1.321$$

$$\Rightarrow .15 > P(T > 1.174) > .10$$

so since pvalue is large cannot reject null hypothesis.  
So there is no evidence that pets have higher cholesterol levels than clinic dogs.

(b) A 95% CI for  $\mu_1 - \mu_2$  is

$$193 - 174 \pm 2.074 \sqrt{\frac{68^2}{26} + \frac{44^2}{23}} \Rightarrow 19 \pm 2.074(16.1870)$$
$$\Rightarrow 19 \pm 33.572$$
$$\Rightarrow (-14.572, 52.572)$$

(c) A 95% CI for  $\mu_2$  is

$$174 \pm (2.074) \left( \frac{44}{\sqrt{23}} \right)$$

$$\Rightarrow 174 \pm 19.028$$

$$\Rightarrow (154.972, 193.028)$$

(d) The primary assumptions are that the two groups of dogs are independent. Also each type of dog should be a SRS from population of all dogs (this is clearly when the chest threat lies). The final assumption is that each is a sample from a normally distributed population (this is the assumption most likely violated).

### Problem 7.107

Let  $\mu_1$  = mean "commitment to adult animals" for evacuees  
 $\mu_2$  = " " " " " " " " " " " non-evacuees

Test  $H_0: \mu_1 - \mu_2 = 0$  (ie no difference)  
vs  $H_A: \mu_1 - \mu_2 \neq 0$  (difference in commitment)

$$\text{test statistic } t = \frac{7.95 - 6.26}{\sqrt{\frac{3.62^2}{116} + \frac{3.56^2}{125}}} = 3.650$$

with  $df = \min(116-1, 125-1) = 115 \Rightarrow$  use  $df = 100$  line

$$3.390 < 3.650$$

Since  $H_A$  is  $\mu_1 - \mu_2 \neq 0$   
p-value =  $2P(T > 3.650)$

$$\Rightarrow .0005 > P(T > 3.650)$$

$$\Rightarrow .001 > 2 P(T > 3.650)$$

so since pvalue  $< .001$  thus means we can reject the null hypothesis. So conclude that there is a difference in "commitment to adult animals" between the groups.

### Problem 7.110 a, b, c

Let  $\mu_1$  = mean number of pins for students  
 $\mu_2$  = mean number of pins for workers

(a)  $H_0: \mu_1 - \mu_2 \geq 0$  (ie students were better)

$H_A: \mu_1 - \mu_2 < 0$  (ie students worse)

$$\text{test statistic } t = \frac{35.12 - 37.32}{\sqrt{\frac{4.31^2}{750} + \frac{3.83^2}{412}}} = -8.954 \text{ (3dp)}$$

with  $df = \min(750-1, 412-1) = 411$  so use  $df=100$  line

since  $H_A$  is  $\mu_1 - \mu_2 < 0$  Pvalue =  $P(T < -8.954)$



by symmetry of  $t$  distribution  $P(T < -8.954) = P(T > 8.954)$

$3.390 < 8.954$   
 $.0005 > P(T > 8.954)$   $\Rightarrow$  Pvalue  $< .0005$   
 $\Rightarrow$  reject  $H_0$ . Therefore experienced workers could complete more pins on average than students.

(b) Because we have large sized samples CLT applies which tells us that  $\bar{X}$  has approximately normal distribution

(c) "an experienced worker" = sample of size 1

so CI is

$$37.32 \pm 1.96 \frac{3.83}{\sqrt{1}}$$

$$\Rightarrow \cancel{37.32} \pm 7.507$$

$$\Rightarrow (29.813, 44.827)$$