

Homework #5 Solutions

(1)

1.104, 1.105, 3.1, 3.3, 3.23, 3.28

Problem 1.104

Let $X =$ "IQ score" X is distributed Normal with mean 100, standard deviation 15.

Below 100 $\equiv X < 100$

$$(a) \quad P(X < 100) = P\left(\frac{X-100}{15} < \frac{100-100}{15}\right)$$

$$= P(Z < 0)$$

$$= 0.5 \quad (50\%)$$

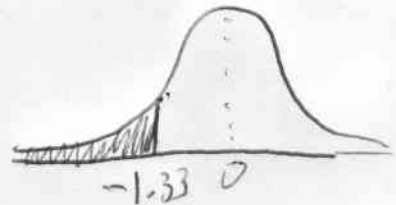


Below 80 $\equiv X < 80$

$$(b) \quad P(X < 80) = P\left(\frac{X-100}{15} < \frac{80-100}{15}\right)$$

$$= P(Z < -1.33)$$

$$= .0918 \quad (9.2\%)$$



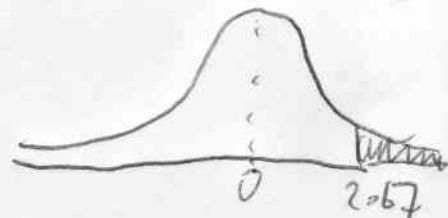
Above 140 $\equiv X > 140$

$$(c) \quad P(X > 140) = P\left(\frac{X-100}{15} > \frac{140-100}{15}\right)$$

$$= P(Z > 2.67)$$

$$= 1 - P(Z < 2.67)$$

$$= 1 - .9962 = .0038 \quad (\approx .4\%)$$

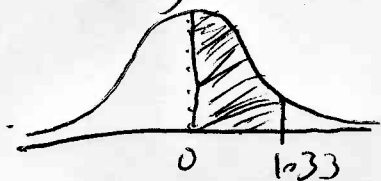


Between 100 and 120 $\equiv 100 < X < 120$

(d) $P(100 < X < 120) = P\left(\frac{100-100}{15} < \frac{X-100}{15} < \frac{120-100}{15}\right)$

(2)

$= P(0 < Z < 1.33)$

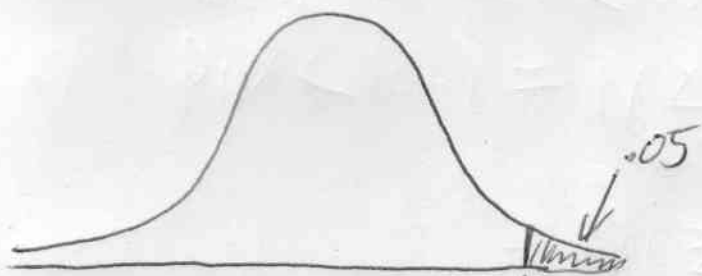


$= P(Z < 1.33) - P(Z < 0)$

$= .9082 - .5$

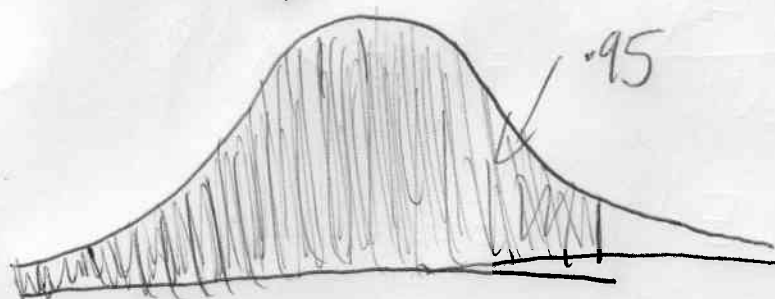
$= .4082$

Problem 1.105



equivalent \updownarrow

what is this value?



From the normal table ^{searching for} $P(Z < z) = .95$

gives $P(Z < 1.64) = .9495$

and $P(Z < 1.65) = .9505$

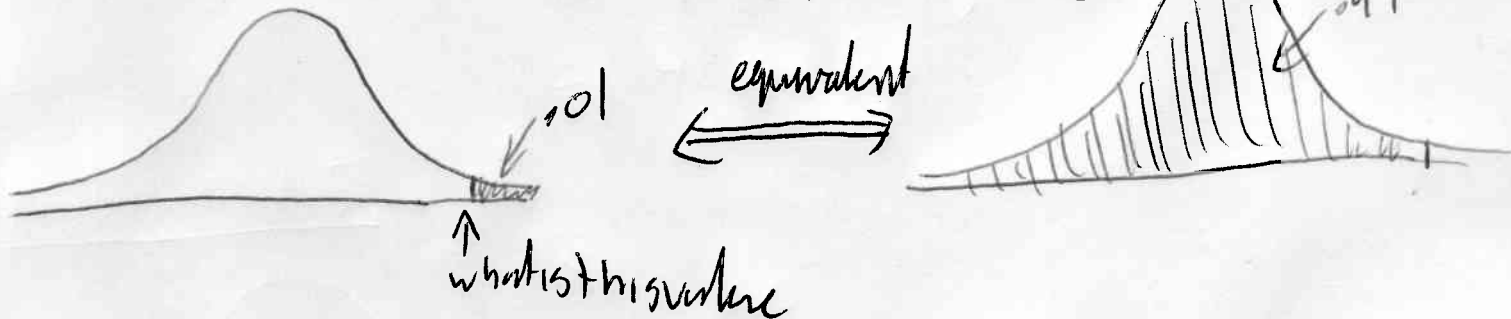
since .95 is about half way between these two values take $z = 1.645$

Need to transform to mean and stdev of original data (3)

so

$$x = z\sigma + \mu = (1.645)(15) + 100 = 124.675$$

$$\text{i.e. } P(X > 124.675) = 0.05$$



From table searching for $P(Z < z) = 0.99$

$$\text{gives } P(Z < 2.33) = 0.9901$$

transforming to mean and sd of original data

$$x = z\sigma + \mu = (2.33)(15) + 100 = 135$$

Problem 3.1

This is not good evidence that cell phones cause brain tumors because it is anecdotal evidence.

Her friends could be related in some other way (ie perhaps ^{they are} exposed more frequently to some pollutant because they live in same area. In addition she

↳ biasing her view off just two non randomly chosen people. ④

Problem 3.3

This is an observational study because the researcher did not have any control over any variable. The explanatory variable is cell phone use. The response variable is whether they had brain cancer or not.

Problem 3.23

| | | | |
|----|----|----|----|
| 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |

The important thing about this problem is how you assign the colors. Note that "randomly" does not mean helter-skelter or just how you feel like doing it. You have to have a method of assigning colors using random number or similar.

↗ The field
a pole location
the numbering ^{and grids} will help us assign colors to the poles

First I decide to assign the 4 blue, then 4 green, 4 white and 4 yellow. How do I do this? - make tickets with numbers 1, 2, ..., 16 on them. Put all the tickets into a box and shake vigorously. Then 1 by 1 I draw tickets from the box. The first four numbers correspond to the four poles which get blue. The next four correspond to green, the next four to white and the remaining four to yellow.

My drawing order:

3, 13, 4, 15, 14, 6, 5, 2, 10, 16, 7, 11, 8, 1, 12, 9

So
 blue : 3, 13, 4, 15
 green : 14, 6, 5, 2
 white : 10, 16, 7, 11
 yellow : 8, 1, 12, 9

| | | | |
|---|---|---|---|
| y | a | B | B |
| a | a | w | y |
| w | w | y | y |
| B | a | B | w |

Problem 3.28

6

- (a) Factors: 1. Time question presented
2. Type of question

levels
Time question presented $\begin{cases} \text{before} \\ \text{after} \end{cases}$ (2)

Type of question asked $\begin{cases} \text{simple fact} \\ \text{computation} \\ \text{word problem} \end{cases}$ (3)

There are $(2)(3) = 6$ different treatments

- trt 1: before : simple fact
- trt 2: before : computation
- trt 3: before : word problem
- trt 4: after : simple fact
- trt 5: after : computation
- trt 6: after : word problem

the six possibilities listed.

(b) Assume we start with 12 classes. Assign each class a number between 1 and 12. Using a computer we draw numbers between 1 and 12 in particular we get

1, 9, 4, 5, 2, 6, 8, 3, 11, 10, 7, 12

Use these to assign treatments as follows.

| | Simple fact | Computation | Word problem |
|--------|-------------|-------------|--------------|
| Before | 1, 9 | 4, 5 | 2, 6 |
| After | 8, 3 | 11, 10 | 7, 12 |

After applying the treatments measure the average math score for all students in the classes who received that treatment.